

# Determination of critical current density in flux creep state for MgB<sub>2</sub>

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## Abstract

We propose a method to determine critical current density  $j_c$  for MgB<sub>2</sub> with flux creep from the real part of AC susceptibility (ACS), which facilitates the determination of  $j_c$  at different DC fields  $B_d$  in temperature range as wide as 5 - 38K. Influence of criterion  $E_c$  on  $j_c$  was studied by varying amplitude ( $B_{ac}$ ) and frequency (f) of AC field. The result shows that it is not proper to obtain temperature dependence of  $j_c$  by measuring only the peak temperature of imaginary part of ACS.

*Key words:*  $j_c$ ; flux creep state; AC susceptibility;

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## 1. Introduction

In the critical state model, the real or imaginary parts of ACS have been connected to  $j_{c0}$ , the  $j_c$  without flux creep [1] by the called ACS method. In addition to the analytical relation [1],  $j_c$  usually is determined based on the critical state model by ACS technique using the equation below:

$$j_{c0}(T_p) = B_{ac}(T_p)/\mu_0 d \quad (1)$$

Nevertheless, due to flux creep, the current density has already decayed before reaching  $j_{c0}$  and its magnitude depends on time and the position in the sample. Here we extend the method to the case with flux creep and determined  $j_c$  in a wider temperature range for a MgB<sub>2</sub> sample. Then influence of the criterion on  $j_c$  was studied.

It is shown that a spatially constant but time dependent  $j(t = 1/f)$  smaller than  $j_{c0}$  inside the sample is a good approximation to describe the dynamics of highly non-linear flux creep [2]. Then the relations between  $\chi'$  and  $j$  can be written formally as:

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$$j_c(f, T_p) = B_{ac}(T_p)/\mu_0 d \quad (2)$$

$$\chi' = -1 + z'/2(B_{ac} \leq \mu_0 j(f)d) \quad (3)$$

$$\chi' = \frac{(-1 + \frac{z'}{2})\cos^{-1}(1 - \frac{2}{z'}) + [-1 + \frac{4}{3z'} - \frac{4}{(3z')^2}](z' - 1)^{1/2}}{\pi} \quad (4)$$

Here  $z' = \frac{B_{ac}}{\mu_0 j(f)d}$ ,  $T_p$  is the temperature at which the imaginary part  $\chi''$  peaks and  $d$  is the half width of the slab. According to the definition, the critical current density is a  $j$  at certain criterion such as electric field  $E_c$ . Hence  $j_c$  extracted from the above equations is in fact the  $j$  at certain criterion. Here the electric field at the surface of the sample is used as  $E_c$ , i.e.  $E_c \equiv E(0)$  [3,4], which can be approximately obtained by:

$$E_c = \frac{1}{4f} \int_0^{1/4f} E(0, t) dt = 4df B_{ac} \quad (5)$$

Here  $E(0, t) = \int_0^d (-\frac{\partial B(x, t)}{\partial t}) dx = 2\pi df B_{ac} \cos(2\pi ft)$ .

Note that the same case also takes place in other methods as long as flux creep is important [5,6] but it was rarely mentioned in previous ACS and VSM methods.

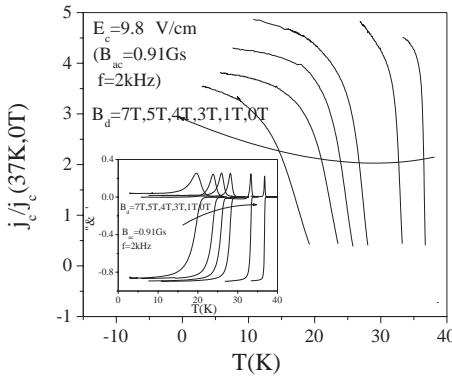


Fig. 1.  $\chi(T)$  (insert) and corresponding  $j_c(T)$  curves at  $B_d = 7T$  and  $5K \leq T \leq 39K$  for  $MgB_2$

## 2. Results and discussions

The sample used here is a sintered  $MgB_2$  rectangular slab. From  $\chi'$  data in the insert of Fig. 1 and equation (2) and (3),  $j_c$  in the range of  $38K - 5K$  are determined and shown in Fig. 1, where  $j_c(0T, 37K) = 10^3 A/cm^2$ . Each  $j_c - T$  curves are determined by a single  $\chi' - T$  curve and easy to obtain in broader temperature range.

Shown in Fig. 2 are the  $j_c(T, E_c)$  curves indicating the influence of  $f$  and  $T$  on the magnetic  $j_c$ . It is apparent that the higher the  $f$ , the larger the  $E_c$ , the higher the  $j_c$ , which coincides with the transport measurements [5,6]. For example,  $j_c(9.8V/cm)$  is more than one order of magnitude larger than  $j_c(0.7V/cm)$  at  $11K$ . If this influence is extrapolated to  $j_c$  measurements by ACS in a wider frequency range, E.G.  $0.1kHz \leq f \leq 10kHz$ , one can expect that  $j_c(10kHz)$  is approximately two orders higher than  $j_c(0.1kHz)$ . The fact that the  $\chi' - T$  curve are dependent on  $f$  is a strong evidence that flux creep is also giant in  $MgB_2$  and could not be explained by any critical state model.

Because  $E_c$  is also proportional to  $B_{ac}$ ,  $B_{ac}$  influences  $j_c$  as well. Shown in Fig. 3 are examples of the influence by  $B_{ac}$ , where it is also seen that a larger  $B_{ac}$  corresponds to a larger  $E_c$  and thus a higher measured  $j_c$ . These experimental data, in addition to the above argument, show that it is not proper to determine temperature dependence of  $j_c$  from  $j(T_p)$  measurement of peak temperature  $T_p$  of  $\chi''$  at different  $f$  or  $B_{ac}$  based on equation (1)[7] because shifting  $T_p$  by changing either  $f$  or  $B_{ac}$  simultaneously changes  $E_c$  as well.

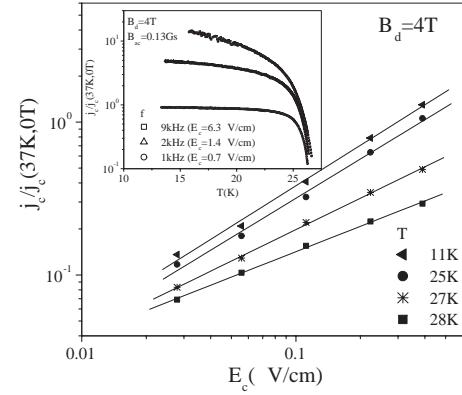


Fig. 2. Influence of  $f$  ( $E_c$ ) on  $j_c$  determination at four different temperatures for  $MgB_2$

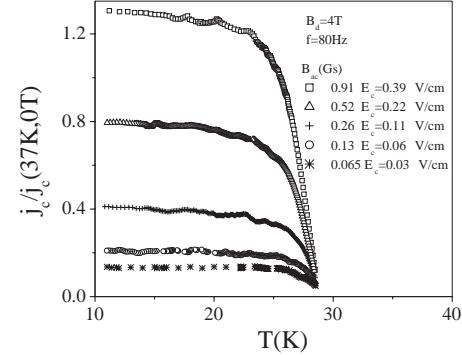


Fig. 3. Influence of  $B_{ac}$  ( $E_c$ ) on  $j_c(T)$  curves in magnetic measurement for  $MgB_2$

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