

# Thermal expansion and ultrasonic measurements of ferroquadrupole ordering in HoB<sub>6</sub>

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## Abstract

Rare-earth hexaboride HoB<sub>6</sub> shows a ferroquadrupole ordering of  $O_{yz}$ ,  $O_{zx}$  and  $O_{xy}$  with  $\Gamma_5$  symmetry at  $T_Q = 6.1$  K accompanied by a structural change from cubic to trigonal. In order to examine the order parameter in HoB<sub>6</sub>, we have performed ultrasonic and thermal expansion measurements. The lattice length along [001] expands  $\Delta L/L_{[001]} = 2.5 \times 10^{-4}$  just below  $T_Q$ , while the length along [111] shrinks appreciably  $\Delta L/L_{[111]} = -4.5 \times 10^{-3}$ . This result confirms the cubic-trigonal distortion observed by neutron scattering experiments.

*Key words:* HoB<sub>6</sub>; ferroquadrupole ordering; ultrasound; thermal expansion

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Rare-earth hexaborides RB<sub>6</sub> with the cubic CaB<sub>6</sub> type structure show various properties due to the spin, orbit and charge degrees of freedom for 4f-electrons [1]. Heavy rare-earth compound HoB<sub>6</sub> with  $\Gamma_5$  triplet ground state show a ferroquadrupole (FQ) ordering at  $T_Q = 6.1$  K and an antiferromagnetic (AFM) ordering at  $T_N = 5.6$  K. The transverse  $C_{44}$  mode of HoB<sub>6</sub> shows a huge softening of 70% around  $T_Q$ . Neutron scattering indicates the crystal structure of HoB<sub>6</sub> changes from cubic to trigonal at  $T_Q$  [2]. These results are described in terms of quadrupole-strain interaction. In order to characterize the ferroquadrupole ordering in HoB<sub>6</sub>, we have performed ultrasonic measurements in magnetic fields and thermal expansion measurements. Phase comparison method was used for the sound velocity measurements. A dilatometric cell based on capacitance method with an accuracy  $10^{-8}$  was employed.

Fig. 1 shows the temperature dependence of the elastic constant  $C_{44}$  of HoB<sub>6</sub> in magnetic fields for  $H//[111]$ . The  $C_{44}$  is measured by transverse ultrasonic

wave propagating along  $k//[110]$  with polarization  $u//[001]$ . Under zero field, the elastic constant  $C_{44}$  shows a pronounced softening about 70% above  $T_Q$ . This softening arises from the coupling of quadrupole  $O_{yz}$ ,  $O_{zx}$  and  $O_{xy}$  to elastic strain with  $\Gamma_5$  symmetry as,  $H_{QS} = -g\tau_5(O_{yz}\varepsilon_{yz} + O_{zx}\varepsilon_{zx} + O_{xy}\varepsilon_{xy})$ . Increasing magnetic field, the softening of  $C_{44}$  is suppressed and the minimum point indicating ferroquadrupole transition shifts to higher temperatures. The softening of  $C_{44}$  in HoB<sub>6</sub> is influenced easily by magnetic fields. The small magnetic field effect in softening of  $C_{44}$  in DyB<sub>6</sub> is contrast to the present results of HoB<sub>6</sub> in Fig. 1 [3].

The inset of Fig. 1 shows a magnetic phase diagram of HoB<sub>6</sub>. Under high fields up to 6 T, the antiferromagnetic transition temperature  $T_N$  decided by specific heat in magnetic fields for [110] shifts to lower temperatures, while the FQ ordering temperature  $T_Q$  shifts to higher temperatures [4]. These behaviors are typical phenomena in other materials showing FQ ordering [5].

Fig. 2 shows the temperature dependence of thermal expansion in HoB<sub>6</sub> along the [001] and [111] directions. The thermal expansion along [001] expands

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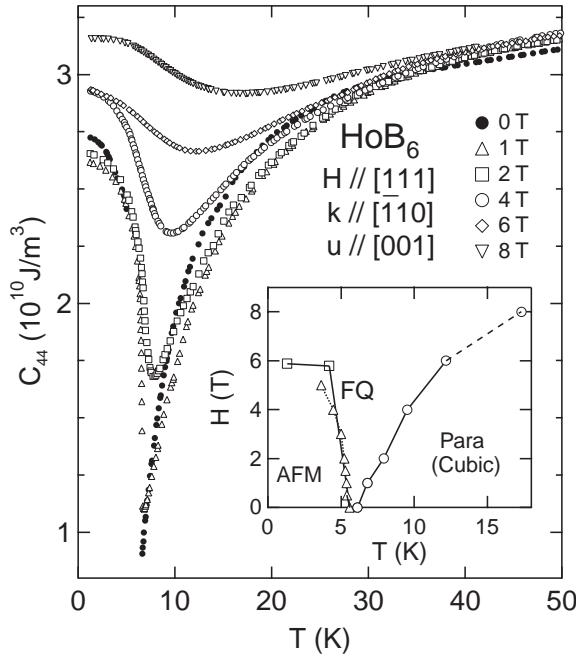
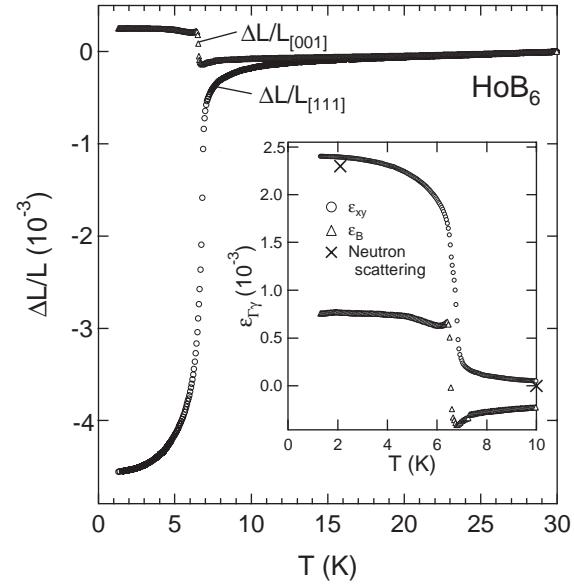


Fig. 1. Temperature dependence of the elastic constant  $C_{44}$  in  $\text{HoB}_6$  under several magnetic fields for  $H // [111]$ . Inset is the magnetic phase diagram of  $\text{HoB}_6$ . The circles ( $T_Q$ ) in phase diagram are decided by temperature dependence of the elastic constant, the squares ( $T_N$ ) by field dependence of the elastic constant and the triangles ( $T_N$ ) by the specific heat in magnetic fields for  $H // [110]$  [3].

$\Delta L/L_{[001]} = 2.5 \times 10^{-4}$ , while along [111] shrinks appreciably  $\Delta L/L_{[111]} = -4.5 \times 10^{-3}$  with decreasing temperature far below  $T_Q$ . The inset of Fig. 2 is the temperature dependence of the spontaneous strains  $\varepsilon_{xy}$ , which means changing the angle between  $x$  and  $y$  axes, and  $\varepsilon_B$ , which means expanding volume, calculated by the experimental results in Fig. 2 using equations  $\Delta L/L_{[001]} = \varepsilon_{zz} = \varepsilon_B/3 + \varepsilon_u/\sqrt{3}$  and  $\Delta L/L_{[111]} = \varepsilon_B/3 + 2(\varepsilon_{yz} + \varepsilon_{zx} + \varepsilon_{xy})/3$ . In the case of cubic-trigonal transition in  $\text{HoB}_6$ , it is naturally expected that tetragonal distortion is irrelevant  $\varepsilon_u = 0$ . Consequently the volume strain is described as  $\varepsilon_B = 3 \times \Delta L/L_{[001]}$ , and the trigonal strain is written as  $\varepsilon_{xy} = (\Delta L/L_{[111]} - \Delta L/L_{[001]})/2$ . The temperature dependence of strains  $\varepsilon_{xy}$  and  $\varepsilon_B$  shows a jump indicating a first order transition at  $T_Q$ . The spontaneous strain  $\varepsilon_{xy} = 2.4 \times 10^{-3}$ ,  $\varepsilon_B = 7.5 \times 10^{-4}$  at 2 K far below  $T_Q$  means the trigonal distortion in addition to the volume expansion. The spontaneous strain  $\varepsilon_{yz} = \varepsilon_{zx} = \varepsilon_{xy} \neq 0$  for trigonal distortion below  $T_Q$  is proportional to the quadrupole moment such as  $\langle \varepsilon_{\Gamma 5} \rangle = N g_{\Gamma 5} \langle O_{\Gamma 5} \rangle / C_{44}^0$ . The distorted angle  $\alpha = 90^\circ + 2\theta$  in the trigonal lattice from  $\alpha = 90^\circ$  in orthogonal axes of cubic is described in terms of the spontaneous strain as  $\varepsilon_{xy} = \sin\theta$ . The neutron scattering of  $\text{HoB}_6$  observed a change of the angle from  $\alpha = 90^\circ$  at 10 K above  $T_Q$  to  $\alpha = 90.264^\circ$  at 2.1



K below  $T_Q$  [2]. This result leads to  $\varepsilon_{xy} = 2.3 \times 10^{-3}$ , which is consistent with the present thermal expansion in Fig. 2.

In this paper, we show the cubic-trigonal distortion in FQ ordering of  $\text{HoB}_6$ . It is now recognized the dilatometry by the capacitance method is a very sensitive probe for the lattice distortion associate with FQ ordering. We are now in progress the thermal expansion under magnetic fields to elucidate field effect for the order parameter of  $\text{HoB}_6$ .

## References

- [1] S. Nakamura, T. Goto, S. Kunii, K. Iwashita, A. Tamaki. J. Phys. Soc. Jpn. 63 (1994) 623.
- [2] A. Dönni, P. Fischer, L. Keller, V. Pomjakushin, Y. Nemoto, T. Goto, S. Kunii. J. Phys. Soc. Jpn. 70 (2001) 448.
- [3] K. Iwashita, T. Matsumura, K. Segawa, S. Kunii. Physica B 186-188 (1993) 636.
- [4] T. Goto, Y. Nemoto, Y. Nakano, S. Nakamura, T. Kajitani, S. Kunii. Physica B 281&282 (2000) 586.
- [5] Y. Nemoto, T. Yamaguchi, T. Goto, O. Suzuki, T. Horino, A. Dönni, T. Komatsubara. Physica B 281&282 (2000) 586.