

# Theory of Resistive Behaviors in Vortex States Induced by Strong Quantum Fluctuation in Type II Superconductors

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## Abstract

Transport data in the vortex liquid regime of underdoped cuprates and organic materials show evidences of strong quantum superconducting fluctuation such as a field-tuned superconductor-insulator transition (FSIT) behavior. Two typical examples of strong quantum fluctuation effects, the FSIT behaviors in dirty films of *s*-wave pairing materials and the field-induced quantum fluctuation effects in  $\kappa$ -(ET)<sub>2</sub> organic superconductors, are discussed through comparison between resistivity data and theoretical curves.

*Key words:* vortex states; field-tuned superconductor-insulator transition; cuprates; organic superconductors

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## 1. Introduction

It is well understood that the fan-shaped broadening of resistance curves in (typically) optimally-doped high  $T_c$  cuprates under nonzero fields ( $H > 0$ ) is due to the thermal superconducting fluctuation [1]. However, the resistivity vanishing in other cuprates with lower  $T_{c0}$  in  $H > 0$  is relatively sharp. This trend in underdoped cuprates means not a weaker but a stronger fluctuation effect: The field-tuned superconductor-insulator transition (FSIT) behavior, observed in strongly underdoped samples [2], cannot occur without a strong quantum superconducting fluctuation [3]. Further, resistivity curves vanishing rapidly much below (appropriately-defined)  $H_{c2}(T)$  or  $T_{c2}(H)$  (and thus, suggesting a strong fluctuation) are seen even in overdoped [4], electron-doped [5] cuprates, and organics [6,7] under *large*  $h = H/H_{c2}(0)$  values.

To understand the sharp resistive vanishing much below  $T_{c2}$  and the FSIT behaviors consistently, it is valuable to, separately from cuprates, first examine such phenomena in conventional materials by combining our theory for the quantum regime [3,8] with ap-

propriate microscopic models for those systems. Here, computed results of resistivity are reported and compared with available experimental data of dirty thin films with *s*-wave pairing [9–11] and quasi 2D organic superconductors [6,7]. Data of underdoped cuprates [2] will be discussed elsewhere[12].

## 2. FSIT behaviors in *s*-wave dirty films

A high field Ginzburg-Landau (GL) theory incorporating microscopic details of *s*-wave dirty amorphous thin films with thickness  $d$  was given in Ref.[3]. In quasi 2D case where  $k_F d > 1$ , the microscopic disorder is measured solely by the reduced sheet resistance  $R_n/R_q$  ( $\propto d^{-1}$ ), where  $R_q = 6.45$  ( $\kappa \Omega$ ) is the quantum resistance, and thus, both strengths of the (quantum) fluctuation and the vortex pinning are enhanced with increasing  $R_n/R_q$ . Results of computed resistance  $R$  are shown in Figs.1 and 2, where the conductance  $R^{-1}$  includes its vortex-glass fluctuation contribution  $R_{vg}^{-1}$  creating the FSIT behavior and a sum of fluctuation contributions excluded from the GL description which should be [3] the origin of the negative magnetoresistance correction *peculiar*[12] to the *s*-wave pairing case

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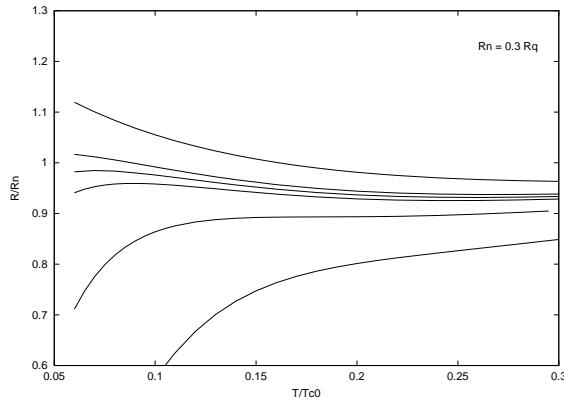


Fig. 1. Low  $T$  resistance ( $R/R_n$  v.s.  $T/T_{c0}$ ) curves computed according to the theory of Ref.[3] assuming an  $s$ -wave dirty film with  $R_n = 0.3R_q$ . The magnetic field is varied from  $h = H/H_{c2}(0) = 0.9$  (top curve) to 0.8 (bottom one), and  $R_c = 0.99R_n$  and  $H_c = 0.865H_{c2}(0)$  are obtained.

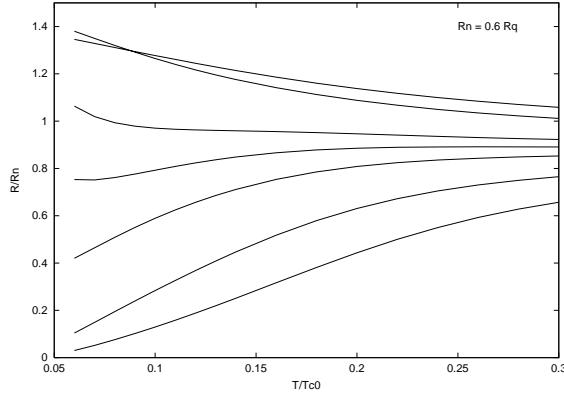


Fig. 2. Corresponding results in  $R_n = 0.6R_q$  to Fig.1. The varied  $h$ -range is from 0.7 to 0.98, and  $R_c = 0.77R_n$  and  $H_c = 0.8H_{c2}(0)$  are obtained.

(see the higher  $h$  curves in Fig.2).

We find through computed curves that, in an intermediate  $T$  range, the  $R(= G^{-1})$ -curve at an *apparent* critical field  $H_c$ , where  $R(T \rightarrow 0)$  takes a  $T$ -independent value  $R_c$ , is insulating if  $R_n/R_q < 0.5$  and is superconducting otherwise. The former and latter behaviors were found in Ref.[9] and Ref.[10], respectively. Further, we find that  $R_c \simeq R_n$  when  $R_n/R_q < 0.5$ , while  $R_c/R_n$  decreases with increasing  $R_n (> 0.5R_q)$ . The former is familiar through data of low  $R_n$  materials [13], while the latter seems to be consistent with a recent report [11].

### 3. Quantum Fluctuation and $H_{c2}$

Fitting to data of organic materials was performed (Fig.3) by assuming the clean limit at the electronic

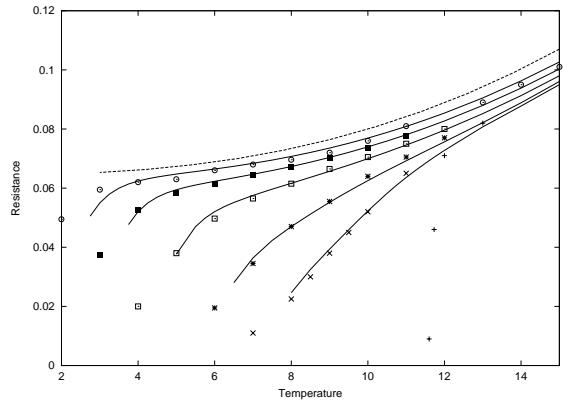


Fig. 3. Fitting results to resistance data [6] in  $H(T) = 1, 2, 4, 6$ , and 8 of  $\kappa$ -(ET)<sub>2</sub>Cu[N(CN)<sub>2</sub>]Br. Theoretical (solid) curves are obtained assuming  $T_{c0} = 12$  (K),  $H_{c2}(0) = 20$  (T), and  $\lambda(0) = 8800$  (A). We note that  $T_{c2}(2(T)) = 11$  (K) and  $T_{c2}(8(T)) = 8$  (K).

level and adding  $R_{vg}^{-1}$  to the conductance. The fan-shaped broadening below 2 (T) is due primarily to the thermal fluctuation, while the higher field behavior following the normal resistance (dashed curve) until rapidly dropping much below  $T_{c2}$  is a consequence of the quantum fluctuation enhanced by increasing  $H$ . Namely, the resistively-determined " $H_{c2}(T)$ " in this case is generally lower than the thermodynamic  $H_{c2}(T)$ . Further, the fact that the above-mentioned high field resistive behavior is visible in materials besides cuprates implies that, contrary to the argument in Ref.[4], it has nothing to do with microscopic ingredients peculiar to the cuprates such as antiferromagnetic vortex core states.

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