

# On the low-temperature maximum of thermal conductivity in cryocrystals

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## Abstract

A model of quantum  $p$  excitations of atoms in cryocrystals is used to describe the observed low-temperature maximum of the thermal conductivity.

*Key words:* cryocrystals; delocalized excitations; quantum transitions; heat conductivity

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At low temperatures, atoms in a condensed matter can exhibit quantum properties. A well-known example of such behavior is a tunneling transition of atoms in a two-well potential, leading to a fractional-power temperature dependence of the heat capacity of glasses [1]. An atom in a crystal, located in an averaged potential of neighboring atoms, can also undergo quantum transitions from the ground  $s$  state to a first excited  $p$  state in its own potential well [2,3]. Such a transition is initiated by interaction of atoms with the phonon modes [4] and results in absorption of energy by the atom and modification of the character of distribution of quantum displacements of the excited atom near a site of the crystal lattice. Due to both translational symmetry of the crystal and inductive interactions of the atom in the  $p$  state with neighboring non-excited atoms, this  $p$  excitation propagates through the crystal by a wide enough  $p$  band, whose bottom is separated from the  $s$  state energy level by a gap  $E_g$ . For example,  $E_g \sim 5 - 6$  K in  $^4\text{He}$  crystals [2–4],  $E_g \sim 20 - 25$  K in solid Ne, Ar, Kr and Xe [5]. The effective mass of an excitation is small and represents about 10 percent of the atomic mass [4,5]. An effective radius of an excited atom of the crystal is somewhat larger than that of an atom in the  $s$  state, so that one can consider a  $p$  excitation as a delocalized point defect of the crystal,

which has an excess energy and is able to transfer the energy through the crystal.

To estimate a low temperature contribution of the  $p$  excitations to the crystal heat conductivity, one can treat them as a gas of particles, whose free path  $\lambda$  is determined by their interactions with the long-wave phonon modes. In such representation, invoking results of the kinetic theory of gases, we express the coefficient  $K_p$  of the heat conductivity as

$$K_p = \frac{1}{3} \frac{C_V}{V} v \lambda, \quad (1)$$

where  $C_V$  is the isochoric heat capacity of the gas of  $p$  excitations,  $V$  is its volume,  $v$  is average velocity of a particle, transferring the energy. As follows from the quantum diffusion theory [6], for wide-band particles at low temperatures,

$$\lambda \sim T^{-7}. \quad (2)$$

The heat capacity of the gas of  $p$  excitations is given by [4]

$$C_V = V \left( \frac{m^*}{2\pi\hbar^2} \right)^{3/2} e^{-E_g/T} \quad (3)$$

$$\times \left[ 1 + \frac{5T}{2E_g} + \frac{5}{2} \left( \frac{T}{E_g} \right)^2 \right]. \quad (4)$$

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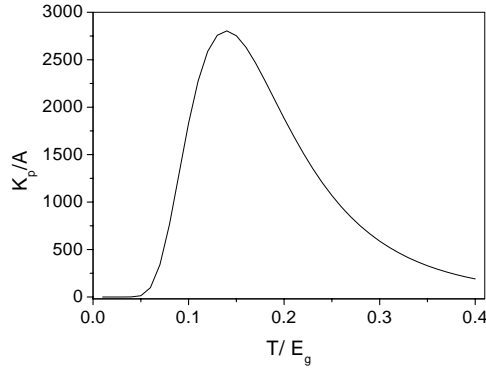


Fig. 1. Reduced thermal conductivity  $K_p(T)/A$  versus reduced temperature  $T/E_g$ .

Then the temperature-dependent part of  $K_p$  is written as

$$K_p = Ae^{-E_g/T} \left( \frac{E_g}{T} \right)^{15/2} \left[ 1 + \frac{5T}{2E_g} + \frac{5}{2} \left( \frac{T}{E_g} \right)^2 \right]. \quad (5)$$

In Fig. 1 we present the temperature dependence of the reduced thermal conductivity  $K_p/A$  in the low-temperature range. The shape of the  $K_p(T)$  curve and the degree of maximal increasing of  $K_p$  are in good agreement with the experimental data [7]. The calculated position  $T_m$  of the maximum of the  $K_p(T)$  dependence is also in good correlation with the observed ones. For example,  $T_m \approx 0.2E_g \approx 1.2$  K for  $^4\text{He}$ ,  $T_m \approx 0.2E_g \approx 4$  K for Ar.

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