

# Transverse Elastic Moduli in Spin-Triplet Superconductor $\text{Sr}_2\text{RuO}_4$

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## Abstract

Transverse ultrasonic measurements have been performed on a single crystal of  $\text{Sr}_2\text{RuO}_4$  across the superconducting transition temperature  $T_c$  ( $\sim 1.40$  K). We found an indication of a jump at  $T_c$  in transverse elastic modulus  $C_{66}$ , which is attributable to the coupling between strains and two-dimensional order parameters(OP) with broken time-reversal symmetry. This leads to additional evidence for the spin-triplet superconductivity with a two-dimensional OP.

**Key words:**  $\text{Sr}_2\text{RuO}_4$ ; Ultrasound; Transverse Elastic Moduli; Two-Dimensional Order Parameter; Broken Time-Reversal Symmetry

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The ruthenate  $\text{Sr}_2\text{RuO}_4$  has the layered perovskite structure of  $\text{K}_2\text{NiF}_4$ -type with a tetragonal crystal point group  $D_{4h}$ . Intense attention has been paid to the ruthenate not only because it is the first example [1] of the non-cuprate layered-perovskite superconductor but also because it shows spin-triplet superconductivity which was proven by the spin susceptibility [2] essentially unchanged across the superconducting transition temperature  $T_c$ . Moreover muon-spin-rotation measurements [3] claim that spontaneous magnetic moment appears in the superconducting state, suggesting a pairing state with broken time-reversal symmetry. Therefore, the symmetry of superconductivity is likely to be of the chiral  $p$ -wave with basically in the form of the superconducting energy gap  $\mathbf{d}(\mathbf{k}) = \hat{\mathbf{z}}(k_x \pm ik_y)$  and in-plane equal-spin pairing [4,5]. Moreover the power-law temperature dependence of the ultrasonic attenuation [6] suggested the existence of nodes in the gap function of  $\text{Sr}_2\text{RuO}_4$ . This state has a two-component order parameter(OP) which belongs to the two-dimensional representation  $E_u$ . Recently, Taillefer, Lupien, and Walker [7] pointed

out that transverse elastic moduli in  $\text{Sr}_2\text{RuO}_4$  may show a discontinuous jump at  $T_c$ . If we find the jump at  $T_c$  in the transverse elastic moduli, it would constitute additional evidence for the  $p$ -wave superconductivity with the two-dimensional OP from ultrasonic experiments [8]. In order to investigate the symmetry of superconductivity in  $\text{Sr}_2\text{RuO}_4$ , we have measured the temperature dependence of transverse elastic modulus  $C_{66}$ .

The single crystal used in this study was prepared by a floating-zone method using an infrared image furnace [9]. We determined  $T_c \simeq 1.40$  K for the present crystal from the onset temperature in elastic modulus, which agrees well with that in ac-susceptibility. The change in sound velocity was measured by a phase-comparison type pulse-echo technique. We measured the in-plane transverse sound velocity propagating along the [100] with the [010] polarization (T1 mode) which corresponds to the transverse elastic modulus  $C_{66}$ . We used ultrasound of 50 MHz generated and detected by a pair of  $\text{LiNbO}_3$  transducers. The elastic modulus  $C_{66}$  was evaluated from the velocity  $v$  using the equation  $C_{66} = \rho v^2$ , where  $\rho$  is the mass density ( $= 5.888 \text{ g/cm}^3$  at 15 K [10]).

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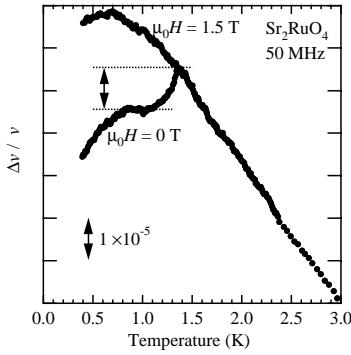


Fig. 1. The temperature dependence of sound velocity shown for both the superconducting state at 0 T and the normal state at 1.5 T. The magnetic field was applied along the  $c$  axis to kill the superconductivity. The jump of  $C_{66}$  at  $T_c$  is indicated by the arrow line, the magnitude of which was as small as  $\Delta v/v = 1 \times 10^{-5}$ .

Temperature dependence of the sound velocity of T1 mode below 3 K in magnetic field  $\mu_0 H$  is displayed in Fig. 1. We determined the absolute value of sound velocity to be  $2.6 \times 10^3$  m/s at 4.2 K by directly measuring the time interval between the subsequent echo signals. In consequence, we obtained the approximate value of 40 GPa for the elastic modulus  $C_{66}$  at 4.2 K. The sound velocity in the superconducting state is evidently small compared with that in the normal state.

For superconductors with a *one-dimensional* OP, the first-order derivative of  $T_c$  with respect to shear strain  $\varepsilon_\Gamma$  is absent since  $+\varepsilon_\Gamma$  and  $-\varepsilon_\Gamma$  give the same energy state. Consequently the transverse elastic modulus exhibits no jump at  $T_c$ . In contrast, for a superconductor with a *two-dimensional* OP with broken time-reversal symmetry, it is not obvious whether  $+\varepsilon_\Gamma$  and  $-\varepsilon_\Gamma$  always give the same energy state or not. We briefly discuss the behavior of elastic moduli in  $\text{Sr}_2\text{RuO}_4$  with a single set of order parameters  $\mathbf{d}(\mathbf{k}) = \hat{\mathbf{z}}(\eta_x k_x + \eta_y k_y)$ . The order parameter has two components, belonging to the irreducible representations  $E_u$ , and its symmetric square is

$$[E_u]^2 = A_{1g} + A_{2g} + B_{1g} + B_{2g}. \quad (1)$$

For point group  $D_{4h}$ , one has the following strain representations:  $A_{1g}(\varepsilon_{xx} + \varepsilon_{yy})$ ,  $A_{1g}(\varepsilon_{zz})$ ,  $B_{1g}(\varepsilon_{xx} - \varepsilon_{yy})$ ,  $B_{2g}(\varepsilon_{xy})$  and  $E_g(\varepsilon_{yz}, \varepsilon_{zx})$ , corresponding to  $(C_{11} + C_{12})$ ,  $C_{33}$ ,  $(C_{11} - C_{12})$ ,  $C_{66}$  and  $C_{44}$ , respectively. Therefore the coupling terms of the free energy read

$$\begin{aligned} F_{\text{so}} = & (g_{A_{1g}}(\varepsilon_{xx} + \varepsilon_{yy}) + g'_{A_{1g}}\varepsilon_{zz})(|\eta_x|^2 + |\eta_y|^2) \\ & + g_{B_{1g}}(\varepsilon_{xx} - \varepsilon_{yy})(|\eta_x|^2 - |\eta_y|^2) \\ & + g_{B_{2g}}\varepsilon_{xy}(\eta_x^*\eta_y + \eta_x\eta_y^*), \end{aligned} \quad (2)$$

where  $g_\Gamma$  is coupling constant with symmetry  $\Gamma$ . Because there is no coupling linear in the strain  $\varepsilon_{yz}$ ,  $\varepsilon_{zx}$

but quadratic in OP in the free energy, the transverse elastic modulus  $C_{44}$  exhibits no jump at  $T_c$  in the two dimensional OP [11]. It is not obvious whether  $(C_{11} - C_{12})/2$  should exhibit a jump at  $T_c$  from this discussion alone since it is not necessarily  $|\eta_x|^2 = |\eta_y|^2$ . In contrast, the elastic modulus  $C_{66}$  should show a step-like decrease at  $T_c$ . In Fig. 1, we can indeed see a jump-like behavior at  $T_c$ . The roughly estimated jump is smaller than  $8 \times 10^{-4}$  GPa, which is shown in Fig. 1. From the magnitude of the jumps at  $T_c$ ,  $|\Delta C_{11}(T_c)| \sim 1.5 \times 10^{-2}$  and  $|\Delta C_{33}(T_c)| \leq 1 \times 10^{-3}$  GPa [12]; it is expected that  $|(g_{A_{1g}} + g_{B_{1g}})| > |g'_{A_{1g}}| \geq |g_{B_{2g}}|$ .

In summary, we measured the transverse elastic modulus  $C_{66}$  across  $T_c$  in  $\text{Sr}_2\text{RuO}_4$ , and observed a jump-like behavior at  $T_c$ . We briefly discussed the behavior of elastic moduli with two-component OP, and we pointed out that  $C_{66}$  is likely to jump at  $T_c$ . If we confirm a jump more clearly in the transverse elastic modulus, it constitutes additional evidence for the p-wave superconductivity with the two-dimensional OP from the ultrasonic experiments.

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