

# Effects of impurities on the magnetic property in copper oxides

Daisuke Matsunaka <sup>a</sup>, Hideaki Kasai <sup>a,1</sup>, Hiroshi Nakanishi <sup>a</sup>, Ayao Okiji <sup>b</sup>

<sup>a</sup> *Department of Applied Physics, Osaka University, Suita, Osaka 565-0871, Japan*

<sup>b</sup> *Wakayama National College of Technology, Gobō, Wakayama 644-0023, Japan*

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## Abstract

We study effects of the nonmagnetic impurities on the magnetic property in the CuO<sub>2</sub> plane of copper oxides. We calculate the spin susceptibility in the normal state, for the CuO<sub>2</sub> plane with nonmagnetic impurities substituted for Cu atoms, on the basis of the d-p model. We take account of the impurity scattering and the Coulomb interaction at each Cu site within the single-site coherent potential approximation and the fluctuation-exchange approximation, respectively. Our result implies that the nonmagnetic impurities suppress the antiferromagnetic spin fluctuations which mediate the superconductivity in high-temperature superconductors.

*Key words:* spin susceptibility ; impurity ; d-p model ; Green's function methods

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Many copper oxides are well-known as high-temperature superconductors (HTSC). They share layered perovskite structures and contain two-dimensional CuO<sub>2</sub> planes in which superconductivity appears below  $T_c$ . Regarding HTSC, evidence has accumulated for an anisotropic energy gap most likely of  $d_{x^2-y^2}$  symmetry. The effects of the Coulomb-enhanced spin fluctuations are believed to play an essential role in HTSC.

For  $d_{x^2-y^2}$  pairing, nonmagnetic impurities in the CuO<sub>2</sub> planes, such as Zn impurity atoms substituted for Cu atoms, destroy the superconductivity and are shown to be pair breakers, producing a finite lifetime for quasiparticles near the nodes and a finite density of states at low energies [1]. It is also known that resonant impurity scattering leads to important effects for the penetration depth [2] and the NMR response [3].

In this paper, we investigate both of effects of Coulomb correlations and the impurity scattering, on the spin susceptibility, within the fluctuation exchange approximation (FLEX) [4] and the single-site coherent potential approximation (CPA) [5] respectively. In order to describe the CuO<sub>2</sub> plane of copper oxides, we adopt the d-p Hamiltonian as follows:

$$\begin{aligned}
 H = & \sum_{\mathbf{k}, \sigma} \left( d_{\mathbf{k}, \sigma}^\dagger p_{\mathbf{k}, \sigma}^{x\dagger} p_{\mathbf{k}, \sigma}^{y\dagger} \right) \\
 & \times \begin{pmatrix} \epsilon_d & \zeta_{\mathbf{k}}^x & \zeta_{\mathbf{k}}^y \\ (\zeta_{\mathbf{k}}^x)^* & \epsilon_p & 0 \\ (\zeta_{\mathbf{k}}^y)^* & 0 & \epsilon_p \end{pmatrix} \begin{pmatrix} d_{\mathbf{k}, \sigma} \\ p_{\mathbf{k}, \sigma}^x \\ p_{\mathbf{k}, \sigma}^y \end{pmatrix} \\
 & + \frac{U}{N} \sum_{\mathbf{k}, \mathbf{k}'} \sum_{q (\neq 0)} d_{\mathbf{k}+\mathbf{q}, \uparrow}^\dagger d_{\mathbf{k}'-\mathbf{q}, \downarrow}^\dagger d_{\mathbf{k}', \downarrow} d_{\mathbf{k}, \uparrow} \\
 & + \sum_{i, \sigma} u_i d_{i, \sigma}^\dagger d_{i, \sigma}
 \end{aligned} \tag{1}$$

where  $\zeta_{\mathbf{k}}^{x(y)} = 2it \sin \frac{k_x(y)}{2}$ .  $u_i = u$ , when an impurity is present at  $\mathbf{r}_i$ . We measure the site energy of  $d(p)$ -orbital  $\epsilon_{d(p)}$  from the Fermi level, which is set to zero. The Green's function of d-electron is given by

$$G_d(k) = \frac{i\epsilon_n - \epsilon_p}{(i\epsilon_n - \epsilon_d - \Sigma(k))(i\epsilon_n - \epsilon_p) - V_k^2} \tag{2}$$

$$\Sigma(k) = \Sigma^{FLEX}(k) + \Sigma^{CPA}(i\epsilon_n) \tag{3}$$

$$V_k^2 = 2t^2(2 - \cos k_x - \cos k_y). \tag{4}$$

The self-energy within FLEX is given as follows:

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<sup>1</sup> E-mail: kasai@dyn.ap.eng.osaka-u.ac.jp

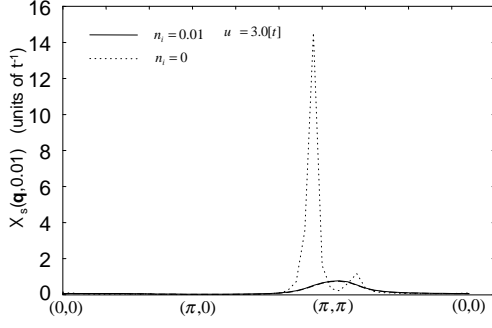


Fig. 1.  $\chi_s(\mathbf{q}, 0.01)$  at the various concentrations of the impurity, at  $T = 0.0047[t]$ , for  $U = 4.2[t]$ ,  $\epsilon_d = -1.7030[t]$  and  $\epsilon_p = -1.9030[t]$ .

$$\Sigma^{\text{FLEX}}(k) = \frac{1}{N} \sum_k V(k - k') G_d(k') \quad (5)$$

$$V(q) = \frac{3}{2} \frac{U^2 \chi(q)}{1 - U \chi(q)} + \frac{1}{2} \frac{U^2 \chi(q)}{1 + U \chi(q)} - U^2 \chi(q) \quad (6)$$

$$\chi(q) = -\frac{T}{N} \sum_k G_d(k) G_d(k + q). \quad (7)$$

where  $G_d(k)$  is the Green's function of d-electron. The self-consistent equation for the coherent potential  $\Sigma^{\text{CPA}}$  is

$$n_i \frac{u - \Sigma^{\text{CPA}}(i\epsilon_n)}{1 + (\Sigma^{\text{CPA}}(i\epsilon_n) - u) G_d(i\epsilon_n)} - (1 - n_i) \frac{\Sigma^{\text{CPA}}(i\epsilon_n)}{1 + \Sigma^{\text{CPA}}(i\epsilon_n) G_d(i\epsilon_n)} = 0 \quad (8)$$

where  $n_i$  is the concentration of the impurity and  $G_d(i\epsilon_n) = \frac{1}{N} \sum_k G_d(k)$ . We solve eqs. 5, 6, 7 and 8, numerically with the Dyson equation, and get  $G_d$  that satisfies them. In these calculations, the vertex correction is neglected consistently. From the self-consistent solution, we calculate the spin susceptibility  $\chi_s(\mathbf{k}, \omega)$  defined by

$$\chi_s(\mathbf{q}, \omega) = \frac{\chi(\mathbf{q}, \omega)}{1 - U \chi(\mathbf{q}, \omega)}. \quad (9)$$

We show the  $q$ -dependence of the imaginary part of  $\chi_s$  at  $T = 0.0047[t]$  in Fig. 1. In the case of  $n_i = 0$ , we see the peak near  $(\pi, \pi)$ . In the case of  $n_i \neq 0$ , the peak is suppressed. The result implies that impurities suppress the antiferromagnetic spin fluctuations which mediate the superconductivity in HTSC.

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## References

- [1] P. J. Hirschfeld, N. Goldenfeld, Phys. Rev. B **48** (1993) 4219; A. V. Balatsky, A. Rosengren, B. L. Altshuler, Phys. Rev. Lett. **73** (1994) 720; P. J. Hirschfeld, W. O. Putikka, D. J. Scalapino, Phys. Rev. B **50** (1994) 10250.
- [2] W. N. Hardy, D. A. Bonn, D. C. Mogan, R. Liang, K. Zhang, Phys. Rev. Lett. **70** (1993) 3999.
- [3] K. Ishida, Y. Kitaoka, N. Ogata, T. Kamino, K. Asayama, J. R. Cooper, N. Athanassopoulou, J. Phys. Soc. Jpn. **62** (1993) 2803.
- [4] S. Koikegami, S. Fujimoto, K. Yamada, J. Phys. Soc. Jpn. **66** (1997) 1538.
- [5] B. Velický, S. Kirkpatrick, H. Ehrenreich, Phys. Rev. **175** (1968) 747.