

# Anomalous Temperature and Disorder Dependence of the Electron-Phonon Scattering Time in Impure Metals

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## Abstract

We have measured the electron-phonon scattering time,  $\tau_{ep}$ , in disordered metals at liquid-helium temperatures, using weak-localization method. The temperature and disorder dependence of  $\tau_{ep}$  is determined for AgPd and AuPd thick films, and  $V_{100-x}Al_x$  alloys. In all three cases, we find an anomalous temperature and disorder dependence of  $\tau_{ep}^{-1} \propto T^2 \ell$ , where  $\ell$  is the electron elastic mean free path. This temperature and disorder behavior cannot be explained in terms of current theoretical concepts for the electron-phonon interaction in impure conductors. Current theory predicts a form of either  $\tau_{ep}^{-1} \propto T^4 \ell$  or  $\tau_{ep}^{-1} \propto T^2 \ell^{-1}$  in the dirty limit, depending on the nature of the defects.

*Key words:* electron-phonon interaction; impure conductors; weak localization

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The electron-phonon (e-ph) interaction in impure conductors is a long-standing problem in condensed-matter physics. The e-ph scattering time,  $\tau_{ep}$ , in the presence of *multiple* elastic impurity scattering has been calculated by several authors for over decades [1–3], but our understanding of the temperature and electron elastic mean free path,  $\ell$ , dependences of  $\tau_{ep}$  is still incomplete. Theoretically and experimentally, different temperature and disorder dependences of  $\tau_{ep}$  have been reported in the literature [4,5]. The situation becomes even less clear in the case of reduced-dimensional systems where the effect of phonon confinement may further complicate the problem. Information about the temperature and mean-free-path dependences of  $\tau_{ep}^{-1}$  will undoubtedly shed light on our understanding of the microscopic interactions of the e-ph process.

In addition to the electron heating measurements [6], systematic information about  $\tau_{ep}(T, \ell)$  can be experimentally obtained from weak-localization (WL) studies, using carefully selected, tailor-made samples cov-

ering a wide range of material characteristics [4,5]. In three dimensions, the total electron dephasing rate that governs the WL effects is given by [7,8]

$$\frac{1}{\tau_\phi(T, \ell)} = \frac{1}{\tau_\phi^0} + \frac{1}{\tau_{ep}} = \frac{1}{\tau_\phi^0(\ell)} + A_{ep}(\ell)T^p, \quad (1)$$

where  $\tau_\phi^0 = \tau_\phi(T \rightarrow 0)$  depends very weakly on temperature, if at all, and is called the saturated dephasing time [5]. The second term in Eq. (1) is due to the e-ph scattering, where  $A_{ep}$  characterizes the strength of e-ph coupling, and  $p$  is an effective exponent of temperature.

In order to improve our understanding of the e-ph interaction in disordered metals, we have in this work measured  $\tau_{ep}$  in a few series of RF sputtered AgPd, and DC sputtered AuPd thick films, and arc-melted  $V_{100-x}Al_x$  alloys. Our samples are polycrystalline, and they are three-dimensional with regard to the electron dephasing length  $\sqrt{D\tau_\phi}$ , where  $D$  is the diffusion constant, that determines the system dimensionality in the WL problem. For each sample, low-field magnetoresistivities between 0.5 and 20 K are measured and compared with three-dimensional WL theoretical predic-

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tions [7] to extract the value of  $\tau_\phi$ . The extracted  $\tau_\phi$  is then least-squares fitted to Eq. (1), yielding the values of  $A_{ep}$  and  $p$ .

We first discuss our experimental temperature dependence of  $\tau_{ep}^{-1}$ . For all samples, the value of  $p$  that we obtained in the above manner is equal or close to 2, suggesting that the experimental e-ph scattering rate is best described with an essentially quadratic temperature dependence (not shown). A quadratic temperature dependence of  $\tau_{ep}^{-1}$  in disordered metals has remained a lasting puzzle for over years [5]. Recently, anew theoretical efforts aiming at resolving this puzzle have been proposed in Refs. [9] and [10].

In addition to the temperature dependence, the  $\ell$  dependence of  $\tau_{ep}^{-1}$  is indispensable in gaining a full explanation of the e-ph interaction in impure conductors. In each series of samples studied in this work, we have “tuned” the amount of disorder (i.e., the residual resistivity  $\rho_0 = \rho(10\text{ K})$ ) by progressively adjusting the fabrication conditions. In the cases of AgPd and AuPd thick films, the value of  $\rho_0$  was tuned by varying the deposition rate; while in the case of  $\text{V}_{100-x}\text{Al}_x$  alloys, the value of  $\rho_0$  was tuned by varying the Al concentration  $x$  from 18 to 26. Within this range of  $x$ , the  $\text{V}_{100-x}\text{Al}_x$  alloys remain single-phased. Our values of  $\rho_0$  are 70–180, 70–230, and 140–210  $\mu\Omega\text{ cm}$  for AgPd, AuPd, and  $\text{V}_{100-x}\text{Al}_x$ , respectively.

What is most striking is that, with the values of  $A_{ep}$  extracted for each series of samples covering a sufficiently wide range of  $\rho_0$ , we observe a totally unexpected linear dependence of  $\tau_{ep}$  on disorder, i.e.,  $\tau_{ep} \propto \rho_0$ . We find that such a linearity holds for all the AgPd, and AuPd thick films, and  $\text{V}_{100-x}\text{Al}_x$  alloys studied. Figure 1 shows a representative plot of the extracted value of  $A_{ep}$  as a function of the reciprocal of  $\rho_0$  for a series of 4000–5000 Å thick AgPd films. This figure clearly reveals that  $A_{ep} \propto \rho_0^{-1}$ , i.e.,  $\tau_{ep}^{-1} \propto \ell$ . Taken together, the observation of Fig. 1 with the above-mentioned  $T^2$  temperature dependence, our result demonstrates an anomalous  $\tau_{ep}^{-1} \propto T^2\ell$  behavior. For a given resistivity of  $\rho_0 = 150 \mu\Omega\text{ cm}$ , we obtain  $\tau_{ep}(1\text{ K}) \approx 1.2 \times 10^{-8}$ ,  $2.5 \times 10^{-10}$ , and  $1.3 \times 10^{-9} \text{ s}$  in AgPd, AuPd, and  $\text{V}_{100-x}\text{Al}_x$ , respectively.

According to the “orthodox” e-ph interaction theory for disordered metals [1–3], that assumes a coherent motion of the impurity atoms with the deformed lattice atoms at low temperatures, one should expect a  $\tau_{ep}^{-1} \propto T^4\ell$  dependence. Recently, it was speculated that, in real metals containing heavy (light) impurities, the impurity atoms might not move in phase with the lattice atoms [11]. The first calculations in consideration of this effect have been done in Ref. [9]. It was found that even a small amount of “static” potential scatterers drastically changes the e-ph-impurity interference, and the relaxation rate is proportional to  $T^2L^{-1}$ , where  $L$  is the electron mean free path with respect to the static

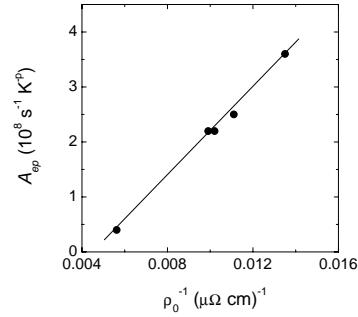


Fig. 1. Variation of  $A_{ep}$  with  $\rho_0^{-1}$  for AgPd thick films. The straight line drawn through the data is a guide to the eye.

impurities ( $L \gg \ell$ ). Experimentally, a  $T^4$  dependence has been observed very recently, in disordered Hf and Ti thin films [12]. However, to the best of the authors’ knowledge, the combined  $T^4\ell$  law has *never* been found in any real conductors thus far. On the other hand, a distinct  $\tau_{ep}^{-1} \propto T^2\ell^{-1}$  dependence has been observed in  $\text{Ti}_{100-x}\text{Al}_x$  and  $\text{Ti}_{100-x}\text{Sn}_x$  alloys [13]. Previously, a  $T^2\ell$  dependence has been observed in two-dimensional Nb thin films [14].

In conclusion, we have found extensive evidence of a  $T^2\ell$  temperature and disorder dependence of  $\tau_{ep}^{-1}$  in AgPd, and AuPd thick films, and  $\text{V}_{100-x}\text{Al}_x$  alloys. This  $T^2\ell$  behavior is unexpected, even qualitatively, in terms of the current theoretical concepts for the e-ph interaction in impure conductors.

The authors are grateful to A. Sergeev and G. Y. Wu for valuable discussion. This work was supported by the Taiwan NSC through Grant Nos. NSC90-2112-M-009-037 and NSC90-2119-M-007-004.

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