

# Novel Superfluid Transitions of $^3\text{He}$ in the Bulk and on the Surface Layer

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## Abstract

The novel superfluid (SF) transitions of  $^3\text{He}$  in the bulk and on the surface layer are studied within the two-stage Fermi-Bose-liquid model of superfluidity in Fermi systems. We argue that the novel superfluidity in  $^3\text{He}$  results from the BCS-like p-wave pairing of fermions and the SF condensations of two-fermion composite bosons. We show that the A-phase is formed both in the bulk and on surfaces at SF pair condensation of triplet composite bosons with parallel spins, while the B-phase is formed only in the bulk at SF single particle condensation of such bosons with antiparallel spins and the surfaces destabilize the B-phase.

*Key words:* Superfluid  $^3\text{He}$ ; novel superfluidity; surfaces

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## 1. Introduction

During the last decades, the superfluid (SF) phase transitions of  $^3\text{He}$  have been studied within the BCS-like Fermi-liquid theories [1, 2]. It is well known that when the liquid  $^3\text{He}$  is cooled at high pressures first it undergoes a second-order phase transition into the SF A-phase at the temperature  $T = T_c$  and then the SF  $^3\text{He}$  undergoes a first-order phase transition at  $T = T_{AB} < T_c$  into the B-phase. These SF phase transitions of  $^3\text{He}$  and the natures of the A and B phases cannot be understood properly in terms of the BCS-like pairing (or Fermi-liquid) theories [3, 4]. Because the BCS-like pairing theories may explain only the precursor second-order phase transition. But the true SF phase transitions (in particular, the first-order phase transition), the specific features of the A-B transition in the bulk and surfaces and the effects of pressure, magnetic field, rotation and surfaces on nucleation processes of the A and B phases in  $^3\text{He}$  remain long-standing mysteries to these theories. We develop in this paper a novel two-stage Fermi-Bose-liquid model of superfluidity in  $^3\text{He}$

[4]. This novel superfluidity results from the BCS-like p-wave pairing of fermions and the SF single particle and pair condensations of attracting two-fermion composite bosons. Here we study the distinctive SF transitions of  $^3\text{He}$  in the bulk and on surfaces within the proper SF Bose-liquid model.

## 2. Precursor BCS-like p-wave pairing scenario

Our first postulate reads as follows: any BCS-like pairing state of fermions (i.e.  $^3\text{He}$  atom) is the precursor state but not SF one. In particular, the BCS-like p-wave pairing of He atoms leads to the formation of the precursor Anderson-Brinkmann-Morel (ABM) state of Cooper pairs with angular momentum  $l = 1$  and spin  $S = 1$  below the temperature  $T_F$ . The equations for the BSC-like gap  $\Delta_F(k)$  and transition temperature  $T_F$  are [1, 2]

$$\Delta_F(k) = - \sum_{k'} V_F(k, k') \frac{\Delta_F(k')}{2E_F(k')} \tanh\left(\frac{E_F(k')}{2k_B T}\right) \quad (1)$$

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$$k_B T_F = 1.14 \epsilon_c \exp[-1/N_F(0)|V_{FL}|], \quad (2)$$

respectively, where  $E_F(k) = [\varepsilon_F^2(k) + \Delta_F^2(k)]^{1/2}$  is the excitation energy of a BCS-like Fermi-liquid,  $\varepsilon_F(k)$  is the normal state energy, measured from the Fermi level,  $V_F(k, k')$  is the pairing interaction between fermions,  $\epsilon_c$  is the cutoff energy for  $V_F(k, k')$  which is constant and equal to  $V_{FL}$  for  $\varepsilon_F(k) < \epsilon_c$ ,  $N_F(0)$  is the density of states at the Fermi surface.

### 3. Superfluid single and pair condensations of two-fermion composite bosons in the bulk and on surfaces

Our another postulate is that the superfluidity of triplet Cooper pairs (i.e. cooperons) in  $^3\text{He}$  is driven by their attractive pair and single particle condensations below the temperature  $T_c = T_B$  and  $T_B^* < T_B$  respectively. In the weak-coupling limit the formation of Cooper pairs and the SF condensations of the composite bosons with total angular momentum  $L = l_1 + l_2 = 0$  and spin  $S = s_1 + s_2 = 2$  occur simultaneously (i.e. automatically) at the same temperature  $T_c = T_F = T_B$ . The SF order parameter  $\Delta_B$  and transition temperature  $T_B$  for the bulk  $^3\text{He}$  liquid are determined from the equations [4]

$$\Delta_B(k) = - \sum_{k'} V_B(k, k') \frac{\Delta_B(k')}{2E_B(k')} \coth \frac{E_B(k')}{2k_B T} \quad (3)$$

and

$$T_B = T_{BEC} [1 + 1.42 \gamma_B \sqrt{k_B T_{BEC} / \xi_{BA}}], \quad (4)$$

where  $V_B(k, k')$  is the interaction between composite bosons,  $E_B(k') = [(\varepsilon_B(k) + \tilde{\mu}_B)^2 - \Delta_B^2]^{1/2}$  is the excitation energy of a SF Bose-liquid,  $\gamma_B$  is the interboson coupling constant,  $\varepsilon_B(k)$  is the kinetic energy of composite bosons,  $\tilde{\mu}_B$  is the chemical potential including repulsive Hartree-Fock energy,  $T_{BEC} = 3.31 \hbar^2 n_B^{2/3} / k_B m_B$ ,  $n_B$  and  $m_B$  are the concentration and mass of composite bosons,  $\xi_{BA}$  is the cutoff energy for the attractive part of  $V_B(k, k')$ .

In a three-dimensional Bose-liquid (with  $\gamma_B < 1$ ) the first-order SF phase transition temperature  $T_B^* = T_{AB}$  has the property  $T/\sqrt{2} < T_{AB} < T_c = T_B$  [4]. The energy gap in the excitation spectrum of such a SF Bose-liquid vanishes at  $T = T_B^* = T_{AB}$ . It means that the SF pair and single particle condensation of attracting composite bosons in the bulk of  $^3\text{He}$  liquid lead to the formation of the A- and B-phases, respectively. So, the A-phase is formed at pair condensation of composite bosons (with  $L = 0$  and  $S = 2$ ) at  $T_B^* < T < T_c$  while the B-phase is formed at single particle condensations of composite bosons (with  $L = 0$  and  $S = 0$ ) at

$0 < T < T_{AB}$ . In a two-dimensional Bose-liquid (with  $\gamma_B < 1$ ) the first-order SF phase transition occurs only at  $T = T_{AB} = 0$  [4]. Thus the A-phase nucleation on surfaces is possible at very low temperature and this phase of  $^3\text{He}$  exists even near absolute zero. While the B-phase did not nucleate on surfaces. This phase can nucleate on the surface layer (where  $T_B^* = T_{AB} \neq 0$ ) at significantly lower temperatures than in the bulk. So, the surface layers play a role similar to a magnetic field or a rotation, which shifts the A-B transition to lower temperatures. The above results agree with experimental findings, such as the A-B transition at  $T = 0.78 T_c$  in the bulk, the decreasing of the A-B transition temperature in  $^3\text{He}$  contained within narrow spaces between thin flat plates and the supercooling of the A-phase to temperatures as low as 0.36 mK (or 0.15  $T_c$ ) [3].

### References

- [1] A.J. Leggett, Rev. Mod. Phys. **47** (1975) 331
- [2] P. Wolfle, The superfluid phases of Helium 3, Taylor and Francis, London, 1990
- [3] P. Schiffer, D.D. Osheroff, Rev. Mod. Phys. **67** (1995) 491
- [4] S. Dzhumanov, Int. J. Mod. Phys. B **12** (1998) 2151